# A Macroscopic Fundamental Diagram for Airplane Traffic: Empirical Findings

Victor L. Knoop, Mark ter Heide, Joost Ellerbroek 26 July 2023 Traffic Flow Theory and Characteristics Midyear meeting

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#### Contribution

- Original claim for the macroscopic fundamental diagram by Daganzo (2007): holds for many things, even your desk
- Modelled and tested for road traffic (many...)
- Other modes in city traffic also included (e.g., Loder, 2021cars & bikes)



- Question: does this extend to 3 dimensional modes?
- With possibly a very large amount of airborne vehicles, can we change air traffic management to macroscopic models?



### Introduction

 With many airborne vehicles, can air traffic management use to macroscopic models?





#### 3D MFD models?

- Start of traffic models for drones and control thereof (e.g., Cummings et al, 2021)
- Control based on MFD (Haddad et al, 2022)
- Theoretical derivation of capacities, checked by simulation: (Aarts et al, 2023)
- Empirical validation is still lacking
- Question: is there a relationship between density and production for air traffic?

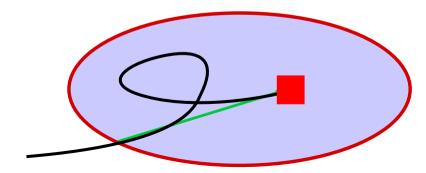


Intersection design: Doole et al, 2021



#### **Definitions**

- 3D extention of Edie's definitions:
  - Density: total travel time / area in space-time
  - Production: effective distance / area in space-time
- In airplane traffic stopping is not an option :)
- Effective distance accounts for detours,
  which are not counted towards effective production





## **Approach**

- Flight data are broadcasted: Automatic Dependent Surveillance-Broadcast (ADS-B).
- The data are recorded by a receiver at the top of the aerospace faculty building of the Delft University of Technology
  - Aggregate over 30 mins
  - density and production
  - Check relationship and interpret





#### **Data**

- Amsterdam Schiphol airport (500,000 flights per year)
- Including surroundings
- Exclude high altitude ("through traffic") keep 5,500 to 19,500 feet
- 42,807 km2
- Select 4 months with various characteristics





#### **Data**

- Range over time of day
- Range over years (covid / non covid)



## **Results**



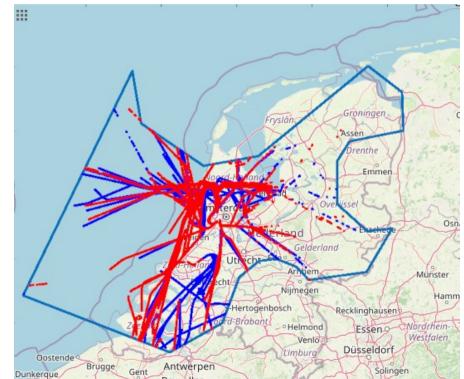
#### Results

- Densities up to 0.0002 planes/km3
- Minimum separation:
  disk of 5 nautical miles radius and 2x 1000 ft altitude
  = 177 km3
  - Density: 1/177=0,0056 planes/km3
- Flow remains increasing
- Effective speed reduces
- Purple fit (Greenshields)



#### Discussion on densities

- Spatially not much of the airspace is used
- Planes cluster around the airport





## **Efficiency**

- Flow reduction: detours or lower speeds?
- Ratio of production and [density times speed]
- Did plane go in one direction?
- Less with higher density, but the reduction of performance (purple line) is much stronger: speed reduction is more important



#### **Conclusions**

- For air traffic, an MFD can be made
- Densities for planes in a larger area do not approach critical density
- Production increases with density, yet flattens (effective speed reduces)
- Main cause: reduction of speed; detours less important





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